Knowledge-based potentials for proteins

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Knowledge based potentials and energy functions are extracted from a number of databases of known protein structures. Recent developments have shown that this type of potential is successful in many areas of protein structure research. Among these are quality assessment and error recognition of folds and the prediction of unknown structures by fold-recognition techniques.

Introduction

The development of energy functions and force fields for studying the behaviour of molecular systems is a major goal in physical chemistry. Prediction of native structures of proteins from amino acid sequences, simulation of the folding process, and calculation of protein stabilities are among the most ambitious goals of contemporary research in biomolecular theory [1].

Research on these topics already has a respectable history, and the difficulties encountered over the past two decades seem to indicate that they might be intractable because of our lack of a suitable theory of molecular interactions, and because of the computational complexities involved. We now, however, have computational tools at hand that enable the recognition of errors in experimentally determined and model structures. Furthermore, fold-recognition techniques are enabling molecular architectures of proteins to be correctly predicted, before their experimentally determined structures are known.

The recent progress has been achieved by new approaches in the development of energy functions. These so-called knowledge-based force fields, or mean force potentials, are derived from experimental data. The basic idea is not new. The molecular structures observed by X-ray analysis or NMR contain a large amount of information on the stabilizing forces within proteins, and statistical analysis has the potential to reveal the underlying rules governing protein stability. In combination with statistical mechanics, the statistical analysis of known three-dimensional structures of proteins is indeed a powerful tool to extract potential functions from a database of known structures.

Several recent reviews on knowledge-based potentials are available (e.g. [2–7,8,9]). Here I concentrate on the characteristics of mean force potentials and the techniques used to investigate their performance and predictive power.

Design principles for molecular energy functions

Construction of energy functions for molecular systems is usually based on several assumptions: first, it is supposed that the behaviour of molecular systems can be captured by a free energy function; second, the potential energy part of the system can be approximated by two-body interactions; and third, molecular structures observed with high frequency correspond to low-energy states. The last statement is a consequence of Boltzmann’s principle, which essentially states that probability densities and energies are closely related quantities. Specifically, in the case of protein-solvent systems, the native structures are thought to correspond to the lowest energy states accessible in equilibrium and the assumption is that it is possible to construct energy functions on the basis of intramolecular and intermolecular atomic pair interactions, whose global minima correspond to native folds.

The construction of potential functions for pair interactions has been attempted from different directions, (see [7] for example). The approach from first principles starts from basic physical laws. Examples include potentials for the electrostatic interactions based on Coulomb’s law, or the Lennard-Jones type potential, whose functional form follows from quantum mechanical calculations. The second type of approach exploits the ever increasing knowledge base of experimentally determined structures relying explicitly or implicitly on Boltzmann’s principle: frequently observed states correspond to low energy states of the system.

The idea to exploit databases for structure prediction has a long tradition [10]. Prediction of secondary structures by observed preferences of amino acids to adopt helix or strand conformations is a popular example. Similarly, statistical potentials have a respectable history. Early attempts to derive potentials from a database of structures were reported almost twenty years ago by Tanaka and

Abbreviations

a—atom a; b—atom b; \( \bar{E} \)—average energy; \( E(r) \)—energy at r; \( \rho(r) \)—probability density at r; \( \bar{E} \)—protein; \( k \)—Boltzmann’s constant; \( r \)—distance between two atoms; s—separation of amino acids; \( \sigma \)—standard deviation; \( T \)—absolute temperature.

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Scheraga [11], and many others have reported subsequent attempts in the intervening period (see e.g. [12–16], and [17–24] for more recent developments).

**Potentials of mean force**

In the following I focus on mean force and related potentials. The general definition of database-derived mean force potentials is [16]

\[ E(r) = -kT \ln[f(r)] \]

where \( r \) is the distance (or some other parameter, like dihedral angles) between two atoms, \( E(r) \) is the energy at \( r \), \( f(r) \) is the probability density at \( r \), \( k \) is Boltzmann's constant and \( T \) is the absolute temperature. Besides \( r \), a particular pair interaction depends on the atom types \( a \) and \( b \) involved (e.g. an interaction between the C\( \beta \) atom of a valine residue and the C\( \alpha \) atom of a glycine), and the separation \( s \) of the respective amino acids along the amino acid sequence [16] (this parameter is important for small separations, for example \( s <10 \); for \( s >10 \), atoms can be considered as free particles):

\[ E_{ab}(s) = -kT \ln[f_{ab}(s)]. \]

\( f_{ab}(s) \) is approximated by relative frequencies obtained from a data base of known structures.

Mean force potentials incorporate all forces (electrostatic, van der Waals, etc.) acting between atoms as well as the influence of the surrounding medium on the interaction. In this form individual potentials contain more or less the same information, but we need the specific information contained in a particular potential that distinguishes it from an average interaction in the system being studied. The redundant information can be captured by a suitably defined reference state. In the case of protein intramolecular interactions a convenient choice for the reference state is [7,16]

\[ E^S(r) = -kT \ln[f^S(r)] \]

which is an average over all atom and residue types. Subtracting this redundant information we obtain the specific interaction

\[ \Delta E_{ab}^S(r) = E_{ab}^S(r) - E^S(r) = -kT \ln \left[ \frac{f_{ab}^S(r)}{f^S(r)} \right] \]

The reference state is a critical feature. Successful applications of mean force potentials largely depend on a suitable reference state.

**A characteristic feature of molecular force fields**

The detailed features of molecular energy functions that govern the folding and stability of proteins are unknown, but some general principles follow from basic physical considerations. Consider a particular protein defined by its amino acid sequence. All possible conformations have associated energy values, and the energy density \( N(E) \) (i.e. the number of conformations per energy interval) characterizes the energy distribution for this protein. By the law of large numbers we might guess that the energy density resembles a Gaussian distribution defined by the average energy \( \bar{E} \) and standard deviation \( \sigma \) (Fig. 1). In fact, we do not know the shape of this distribution, but every distribution has an average and a standard deviation, and we can use these numbers to normalize energy values [7,25**,26**]. \( E \to (E - \bar{E})/\sigma = z \) (these normalized numbers are called z-scores). \( \bar{E} \) and \( \sigma \) are sequence-specific parameters, but they are independent of any particular conformation, as they are average quantities in conformation space.

From the principles of statistical mechanics we know that the energy of the native structure has to be much lower than the average energy and it has to have the minimum energy among all (accessible) conformations. In other words, a native fold has a large negative z-score [7,25**,26**]. Energy functions designed for protein–solvent systems must have the same property. In fact, this principle is very useful in judging the quality of molecular force fields, as the z-scores depend on the energy function employed [25**].

The structures of several hundred proteins are known and the energy \( E_i \), as defined by some energy function, can be calculated for each protein \( i \). What is the significance of the energy of a particular conformation and what does it tell us about the quality of the energy function? To get an answer we have to relate \( E_i \) to the energy distribution of the respective sequence in conformation space [7]. This can be done by estimating \( \bar{E}_i \) and \( \sigma_i \) so that energies can be transformed to z-scores.

As \( \bar{E}_i \) and \( \sigma_i \) are average values, they can be estimated from a small sample of conformation space. A popular sampling strategy is to derive fragments from the known protein structures [18,27,28,29**,30*,31*]. This procedure has several drawbacks (e.g. the sample space for larger proteins is very small), which can be avoided when the structures are joined to a polyprotein [25**,26**].

As an example, Fig. 1 shows the mean force energy density of lysozyme 1LZ3 (PDB code) obtained from a polyprotein. The average performance of an energy function over the set of known protein structures can be expressed by the average score

\[ \bar{z} = \frac{\sum z_i/n}{n} \]

over the individual proteins, where \( n \) is the number of proteins in the test set.
Knowledge-based potentials for proteins

Fig. 1. Energy density of the sequence of lysozyme (PDB code 1lz3) derived from a polyprotein. The total number of conformations is ~50,000. The arrow marks the position of the native fold of 1lz3.

Extraction of mean force potentials from a data base

Mean force potentials are compiled by extracting relative frequencies from a database of protein structures. Several problems are involved in this process. Perhaps the most serious one arises from low counts. In the case of potentials depending on s, the average number of counts is ~100. For rare amino acid pairs like methionine and tryptophan this number is close or equal to zero. Approximation of functions on the basis of such a small number of counts is difficult or impossible in general, but methods have been developed to approximate \( f_{\text{abs}}(r) \) in cases of extremely low counts [16].

The performance and predictive power of mean force potentials depend on a few critical parameters. For example, for distances \( r > 30 \AA \), frequencies are dominated by the large proteins in the database. What is a useful cut-off distance at which to truncate potentials? A reasonable value can be found by calculating the average score \( z \) as a function of cut-off distance. For Cβ-Cβ interactions \( z \) increases (in absolute value) up to 20 Å [25*]; in other words, the information content is maximized when potentials are compiled up to distances of 20 Å.

The dependence of \( z \) on other interesting parameters can also be determined in this way [25*,31*]. How does the quality of potentials depend on the number of proteins in the database? \( z \) as a function of database size follows an exponential saturation. Increasing the database from 50 to 100 proteins yields a 30% increase in \( z \), whereas between 200 and 250 proteins the gain is only 5% [25**]. How are intramolecular pair interactions related to protein–solvent interactions? The scores \( z \) obtained for the individual terms are of comparable size (-6.8 for Cβ pairwise and -6.2 for protein–solvent interactions), but when the two terms are combined the scores increase significantly to -9.66 (M Jaritz, MJ Sippl, unpublished data). In other words, the information contained in intramolecular pair interactions is quite different from protein–solvent interactions and both components are important. Another problem concerns the information contained in pair interactions compiled from different types of atoms. The score of -5.0 for Cα–Cα potentials is less significant as compared to -6.76 for Cβ–Cβ interactions. Their combination scores at an intermediate value of -6.2, in other words, the information contained in these terms is highly redundant (M Jaritz, MJ Sippl, unpublished data).

Our current implementation of mean force potentials consists of pair interactions among all backbone atoms (N, Cα, C, O) and Cβ, and an explicit term for protein–solvent interactions [7,8]. As discussed above, the polyprotein technique has been extensively used to optimize the performance of this energy function [25**,31*].

Applications

Mean force potentials have been successfully applied to various problems in structural biology, such as recognition of errors in experimentally determined structures or the prediction of protein folds by sequence/structure combination.

Detection of errors in protein structures

In several cases errors have been detected in experimentally determined structures [32,33]. Some of the faulty structures have been deposited with the Brookhaven data bank [34] where the faults remained undetected for years, indicating that the criteria used to judge the quality of experimentally determined structures failed in these cases. With the advent of several new programs the situation has improved considerably [26**,35–37]. Native folds have mean force z-scores in a characteristic range, and the energy distribution within native folds shows a characteristic pattern. Erroneous and deliberately misfolded structures are detected by their poor scores and unusual energy distributions [26**]. Because mean force calculations can be done on reduced sets of atoms it is possible to analyze structures where only the Cα backbone is available.

Fig. 2 shows the energy graphs of two experimentally determined structures, photoactive yellow protein and lysozyme (PDB codes 1phy and 2lh2, respectively). Only the Cα coordinates of these structures were deposited with the Brookhaven protein data bank. The z-score for 2lh2 of -8.2 is typical for native structures, but the z-score for 1phy (-1.6) points to an erroneous fold, and the energy graph of 1phy shows that the inter-
232 Theory and simulation

actions in this molecule are unfavourable. The z-scores and energy graphs were calculated using the program PROSA-II [26*] (PROtein Structure Analysis), which is available from gundi.came.sbg.ac.at by anonymous file transfer protocol (ftp).

Quality assessment is an important tool for the judgement of experimental structures and it is a fundamental prerequisite for protein structure theory in general. Prediction of protein structures from amino acid sequences will necessarily fail if faulty structures cannot be distinguished from genuine native folds [38].

**Fig. 2.** Energy graphs for (a) photoactive yellow protein (PDB code 1pby) and (b) lysozyme (PDB code 21zh) generated by PROSA-II [26*]. The graph of 21zh is typical for native folds, but that for 1pby is problematic.

**Fold recognition**

Proteins frequently have similar three-dimensional folds even in cases where no homology is discernible on the sequence level [39**.40**]. It is expected that in a substantial number of cases the unknown structures of protein sequences resemble some known fold. By combining sequences with structures it should be possible to identify such coincidences [41], and there has been considerable progress in the development of fold recognition techniques over the past few years [41–49,50**].

There are three critical components of fold recognition techniques: first, energy functions or parameter sets providing a reasonable description of protein–solvent systems; second, techniques producing useful alignments between sequences and structures; and finally, criteria for identifying native-like sequence/structure combinations [49].

The performance of fold recognition techniques is documented by several detailed case studies [41–49,50**] and several methods are able to recognize distant relationships, such as the similarity between the ADP-ribosylation factor and Ras p21 [49]. Using a database of 150 pairs of proteins related in structure, but unrelated or distantly related in sequence, our implementation based on mean force potentials successfully identifies the related fold in roughly one out of three cases (MJ Sippl, unpublished data).

The most serious challenge testing our current ability to design fold-recognition techniques was the recent prediction experiment organized by J Moult and others. Sequences of several proteins were collected from laboratories that were close to solving the respective structures. Predictions for the individual targets were accepted until the structure was solved and finally the quality of the predictions was judged by a team of assessors. The folds of several proteins were correctly identified by various groups employing fold recognition and/or multiple sequence alignment techniques ([51**] and T Hubbard, personal communication; an issue of *Proteins* dedicated to this prediction experiment is scheduled for 1995).

In some cases the predictions were close to atomic resolution. For the replication terminating protein (PDB code rtp), no homologous sequence could be found by sequence comparison techniques. Fold recognition using mean force potentials suggested the structure of histone (PDB code 1hist) to be a good model for the fold of this protein. The prediction was correct: replication terminating protein and histone indeed have very similar structures. Moreover, the alignment was of excellent quality. Gaps were inserted correctly and the residues of replication terminating protein were placed at the appropriate positions in the histone structure. For the propiece of subtilisin, fold recognition predicted the structure of ferredoxin (PDB code 2fxd). The two structures can be superimposed to a root mean square error of 3.5 Å.

A critical point in fold recognition concerns the quality assessment of a particular model. Any sequence can be combined with any structure. But the question is whether a particular combination corresponds to a useful model that is to some degree similar to the unknown fold of the respective sequence. An important result is that the energy calculated from a model can be misleading. Rather, the energy of the model has to be compared to the energy distribution in conformation space [7,49]. This can be achieved by calculating z-scores as described above.
Genome sequencing projects produce a large number of new sequences. For approximately half of the new genes discovered a biological role or function can be assigned by sequence comparison. The biological information contained in the remaining sequences is not accessible. In a recent large-scale fold recognition study on the 483 genes found in the central gene cluster of *Caenorhabditis elegans* chromosome III, using a data base of 263 known structures, putative models for the unknown folds of 20 sequences have been obtained (M Braxenthaler, MJ Sippl, unpublished data). In light of the successful blind predictions described above, the study demonstrates that fold recognition generates valuable structural and functional information for otherwise uncharacterizable genes and that large-scale applications are computationally feasible.

### Protein stabilities

A vital requirement for rational protein engineering and design is the ability to predict the effect of amino acid replacements on the stability of proteins. In some cases experimental results are well documented. In the case of barnase, Alan Fersht's group has collected a large number of ΔΔG values for various mutations ([52]; ΔΔG is the change in stability between wild-type and mutant protein). As shown in Fig. 3, ΔΔG values calculated from mean force potentials correlate well with measured data (M Hendlich, MJ Sippl, unpublished data).

In other cases the correspondence is less satisfying. Proteins are represented by their Cα backbones only and it is assumed that the Cα backbone is not changed by amino acid replacements. Hence, the present calculations contain assumptions and approximations that may be valid in some situations but may be too crude in others. The applicability of knowledge-based potentials in the design of sequences that fold into predefined structures, a problem closely related to protein stabilities, has been investigated by Jones [53**].

### Ab initio prediction

The long-range goal of force-field development is the *ab initio* prediction of protein structures solely from the information contained in amino acid sequences by energy minimization and folding simulations. Some preliminary studies on small proteins have been performed (e.g. [8*,54,55*,56*]). For example, calculations on thy-mosin β4 are in good agreement with models obtained from NMR studies [54], and computations on the Antenapedia peptide, a small three-helix bundle, come close to the observed structure [8*].

### Conclusions

Knowledge-based force fields have matured into useful tools, providing the basis for powerful techniques in many areas of research into protein structure. They will help to identify the function of protein sequences and aid the determination of their structures. In spite of these successes, the development of force fields and associated methods, like fold recognition, is still at the beginning and there are several problem areas where improvements are possible.

It is clear that *ab initio* prediction, reliable estimation of ΔΔG values, molecular docking and other problems in structural biology require a more detailed representation of molecular structures and atomic interactions than is currently available. The development of such force fields remains a major challenge.
Acknowledgements

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References and recommended reading

Papers of particular interest, published within the annual period of review, have been highlighted as:
• of special interest
** of outstanding interest

A program to recognize erroneous folds or faulty parts of structures obtained by X-ray or NMR analysis or by modeling studies. The program, PROSA-II, is available via anonymous ftp (file transfer protocol) from gundl.came.sbg.ac.at.
29. Kocher JPA, Rooman MJ, Wodak SJ: Factors influencing the ability of knowledge based potentials to identify native sequence-structure matches. J Mol Biol 1994, 235:1598-1611. These authors evaluate the predictive power of various knowledge-based potentials and statistically derived parameters. A potential based on side-chain centroids is found to score highest in the evaluation scheme they define.
The quality of knowledge-based potentials depends on the number of protein structures available for statistical analysis. Sparse data pose a problem, especially for the rare amino acids. Using a weighting scheme, based on amino acid mutation frequencies, potentials of similar amino acids are combined to a single type.
When pair potentials are combined with solvent terms the predictive value of the energy function increases almost twofold, demonstrating the complementary nature of these energy terms.


